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## STUDY OF THE STABILITY OF THE REGULATOR BALANCING ROBOT NI MINDSTORMS

**Abstract.** The article presents the results of studying the steady state of a balancing robot when the control is carried out in a closed state. The synthesis of the controller's coefficients was carried out by estimating the root of the characteristic equation and the linear quadratic regulator. Under the action of the PID controller, algorithms for controlling the robot servos were compiled. The results of the experimental studies allowed us to construct transient characteristics in a closed robot control system while balancing the state of the robot in a steady state and in motion.

**Evaluation of the stability of the robot.** The control system of the balancing robot is asymptotically stable if its steady-state value at the time of its movement or at the moment of stopping will tend to zero regardless of the initial conditions, in the absence of input influences:  $\lim_{t \rightarrow \infty} x(t) = 0$ . It is assumed that the movement of the robot is described by a standard equation of the form:  $\dot{x}(t) = Ax(t) + Bu(t)$  [1]. In order for the robot to be asymptotically stable, it is necessary and sufficient that the real part of all the eigenvalues of the matrix be negative [2-6].

Feedbacks object state control. Let us consider that the robot under the study of a control object is a closed system, the block diagram of which is shown in Figure 1. The feedback control action is determined by the product of the proportionality coefficient  $K$  and the difference between the desired values and the measured values.

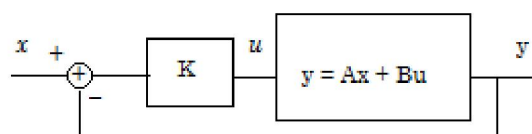


Figure 1 Feedback control

The control action and the status of SIS threads shown in Figure 1 describe the following equations:

$$\begin{aligned} u(t) &= -K(y(t) - x(t)), \\ \dot{x}(t) &= (A - BK)y(t) + BKx(t). \end{aligned} \quad (1)$$

It is necessary to maintain the system under the study of a steady state by dividing by the count value of the matrix  $K$ . Changing these values entails a change of b-governmental numbers of the matrix  $(A - B * K)$ . For sustainable regulation of a closed robot system, it is necessary for it to be controlled. The system will be controllable if the rank of the matrix  $M$  coincides with the rank of the matrix  $A$ . Here  $M_c = [B, AB, \dots, A^{n-1}B]$  you can use the ctrb command to determine manageability in the ControlSystemToolbox environment. There are 2 main methods for calculating feedback coefficients:

1) Calculation of the desired roots. The method describes the calculation of the coefficients  $K$  with the creation of the desired eigenvalues of the matrix  $A - B * K$ . In the ControlSystemToolbox for the calculation, you can use the place function.

**Example 1.**  $K$  coefficients are described in the first communication system with closed CONCRETE and GOVERNMENTAL parameter values  $A = [0, 1; -2; -3]$  and  $B = [0; 1]$ . Pole values are  $[-5, -6]$ .

$$\begin{aligned} & \gg A = [0, 1, -2, -3]; B = [0, 1]; \\ & \gg poles = [-5, -6]; \\ & \gg K = place(A, B, poles) \\ & K = 28,0 \ 8,0 \end{aligned}$$

2) Linear square regulator  $M$  is received by calculating the coefficients of the matrix  $K$  on the basis of minimizing the value of the functional  $J$  calculated in the following form:

$$J = \int_0^{\infty} (x(t)^T Q x(t) + u(t)^T R u(t)) dt$$

. Parameters are adjusted by selecting the weight matrices of the state  $Q$  and the input action  $R$ , which are selected on the basis of the physical nature of the processes. The ControlSystemToolbox application can use the `lqr` functions to calculate a controller.

Example P 2.  $A = [0, 1; -2, -3]$ ,  $B = [0; 1]$ ,  $Q = [100, 0; 0, 1]$ ;  $R = 1$ .

$$\begin{aligned} & \gg \lambda = [0, 1, -2, -3]; B = [0, 1]; \\ & \gg Q = [100, 0; 0, 1]; R = 1; \\ & \gg K = lqr(A, B, Q, R) \\ & K = 8,198 \ 2,137 \end{aligned}$$

The control of the servos of the robot is carried out to generate the desired movement of the robot. For this purpose, the PID controller is most often used [16], i.e. a device in the feedback circuit used by an open-loop control system to generate a robot control signal. The PID controller generates a control signal which is the sum of 3 terms, the first of which is proportional to the input signal, the second is the integral of the input signal and the third is the derivative of the input signal.

The purpose of the PID controller is to maintain a given value  $x_0$  of a certain value  $x$  by changing another value of  $u$ . The value of  $x_0$  is called the “setpoint”, and the difference  $e = (x - y)$  is called the “non-residual” or mismatch. The output signal of the regulator  $u$  is determined by three terms:

$$u(t) = P + I + D = K_p e(t) + K_i \int_0^t e(\tau) d\tau + K_d \frac{de}{dt}, \quad (2)$$

where  $K_p$ ,  $K_i$ ,  $K_d$  are proportional, integral and differential components of the regulator respectively.

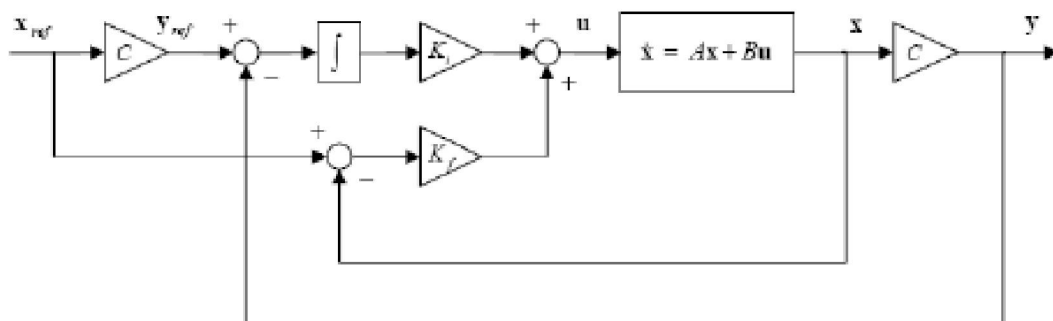


Figure 2 - PID controller

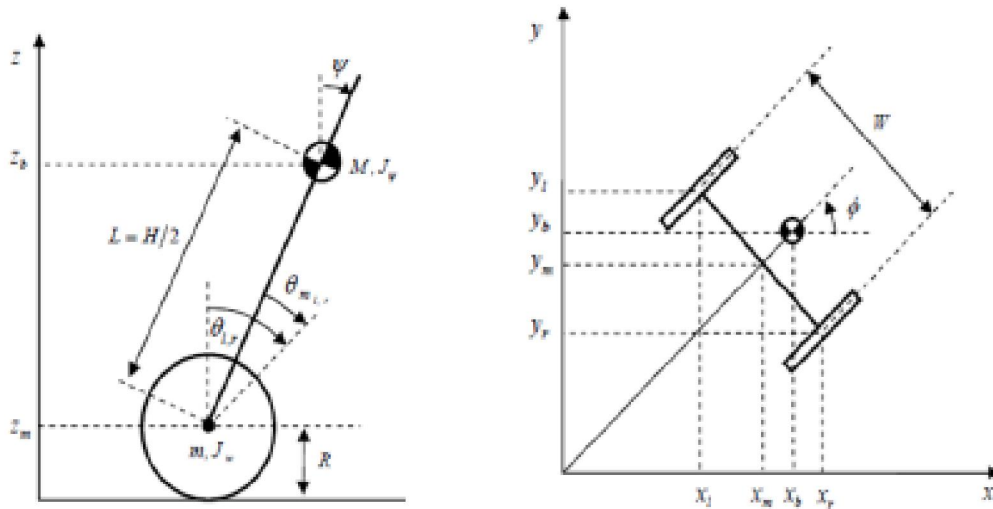


Figure 3 Model Parameter Designation

Figure 3 shows the model parameters indicated for robots: mobile robots of the “Motobot” type [2] and a balancing robot of the “Segway” type [3]. For use in specific studies below are the values of their parameters:

- $g = 9.81 \text{ (m / s}^2\text{)}$  acceleration of gravity;
- $m = 0.03 \text{ (kg)}$  wheel weight;
- $R = 0.035 \text{ (m)}$  wheel radius;
- $J_w = mR^2 / 2 \text{ (kgm}^2\text{)}$  the moment of inertia of the wheel;
- $M = 0.6 \text{ (kg)}$  body weight;
- $W = 0.14 \text{ (m)}$  body width;
- $D = 0.04 \text{ (m)}$  body thickness;
- $H = 0.144 \text{ (m)}$  body height;
- $L = H / 2 \text{ (m)}$  distance to the center of mass from the axis of the wheels;
- $J\Psi = 2 \text{ (M * L) / 3 (kgm}^2\text{)}$  the moment of inertia of the body is tilted;
- $J\phi = M \text{ (W}^2 + \text{D}^2) / 12 \text{ (kgm}^2\text{)}$  rotational moment of inertia;
- $J_m = 10^{-5} \text{ (kgm}^2\text{)}$  the moment of inertia of the engine;
- $K_b = 0.468 \text{ (V * s / rad)}$  is the counter-emf constant;
- $K_t = 0.317 \text{ (N * m / A)}$  is the motor torque constant.

Now we know everything to compile the source code of the program for organizing the movement of the robots. Let's call this program “Segway”. First of all, we compose the main control circuit of the robot. The diagram shown in Figure 4 reflects the main window of the program. The key blocks of the program are described above when they conducted an experimental study on assembling a Motobot robot. The rest of the schemes are contained in the nxtway\_block.

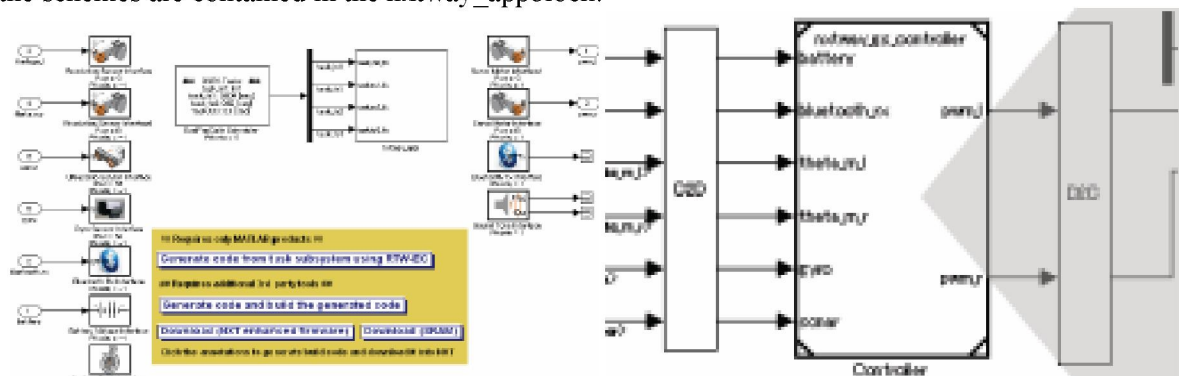


Figure 4 - The program «Segway» (left)  
for the organization of the movement of the robot with the controller (right)

Figure 5 shows a general diagram of the model with all adjustable registrable inputs/outputs. Shown here are the signals that transmit data on the record, which is conducted via Bluetooth protocol.

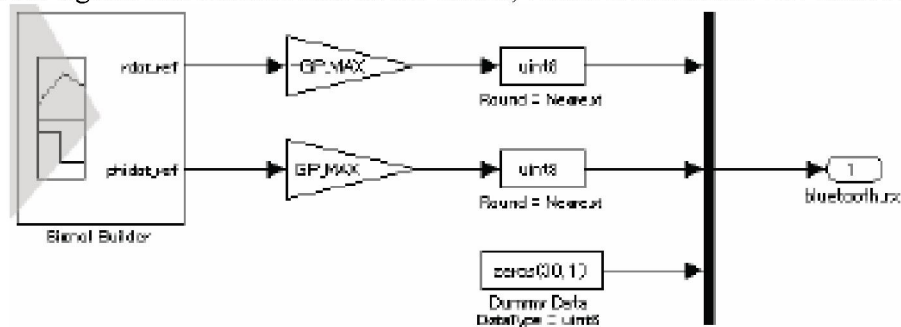


Figure 5 - Control generator diagram

The results of the study made it possible to examine some of the constituent blocks of the robot model in details. ReferenceGenerator is a unit that transmits and limits control actions on the controller. The “Controller” shown in Figure 4 is the block designating the NXT controller. On the left side there are blocks that serve to receive data from sensors, encoders and Bluetooth. On the right side there are blocks that serve to transmit signals to the engines and Bluetooth (Figure 6). The controller unit operates in the discrete time system, and the model unit operates in continuous time mode; therefore, it is necessary to convert the transmitted values.

Figure 7 shows the “NXTway-GS” subsystem, consisting of sensors, drivers, and a linearized model of the robot. It converts the type of input data signals into real values. The subsystem calculates the dynamics of the robot, and displays the recorded data of the results after performing the data sampling procedure. This subsystem defines the parameters of the environment of the robot.

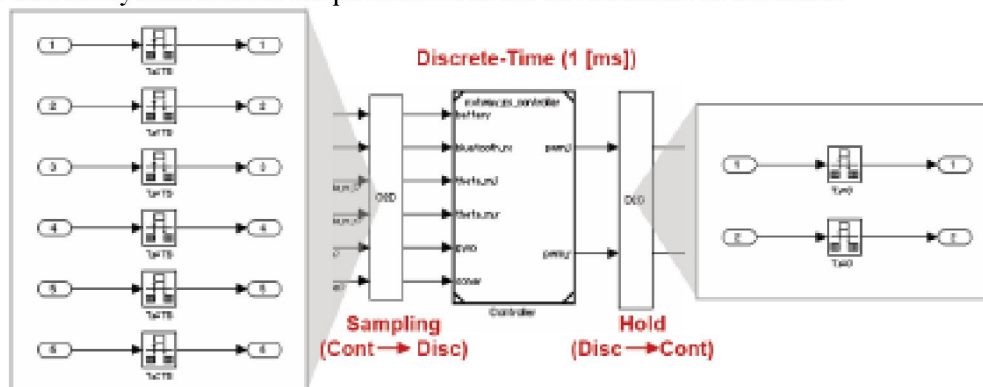


Figure 6 - Circuits of ADC and DAC blocks in models for signal conversion

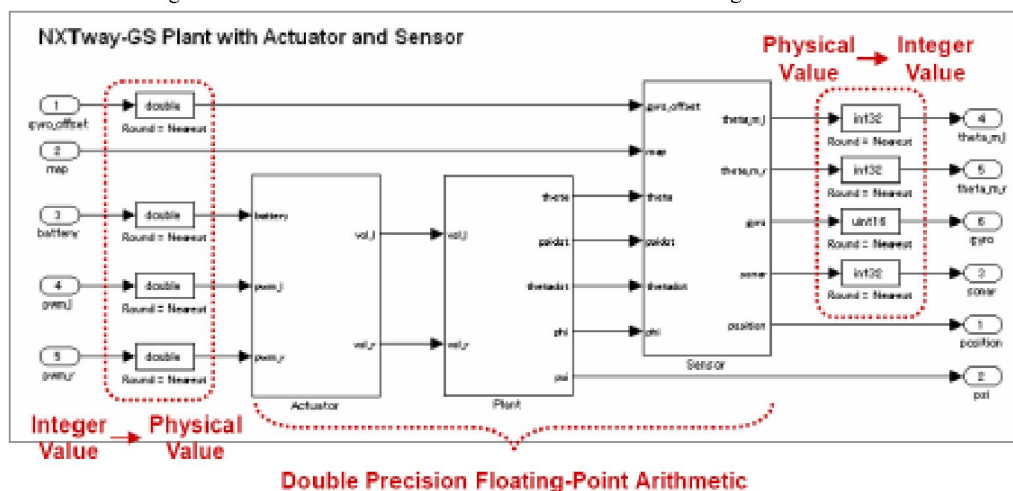


Figure 7 - Scheme servo control depending on the testimony sensors development

The block shown in Figure 7 “Actuator” is a subsystem that converts the power set by the controller to the voltage supplied to the motors. Designated block «Plant» is the model described by equations of double inverted pendulum taking into account the calibration of the gyroscope.

The “Sensor” block converts the values obtained on the state of the model into the output signals of the sensors. Additionally, the distance to obstacles obtained from the ultrasonic distance sensor is calculated. This information may be used for detecting obstructions and avoid collisions with them.

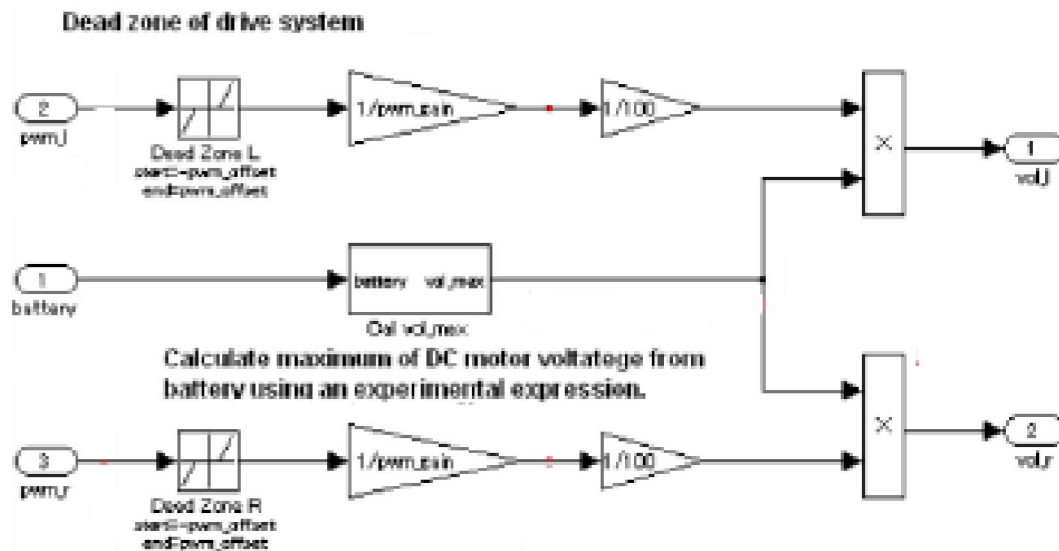


Figure 8 - Drive subsystem

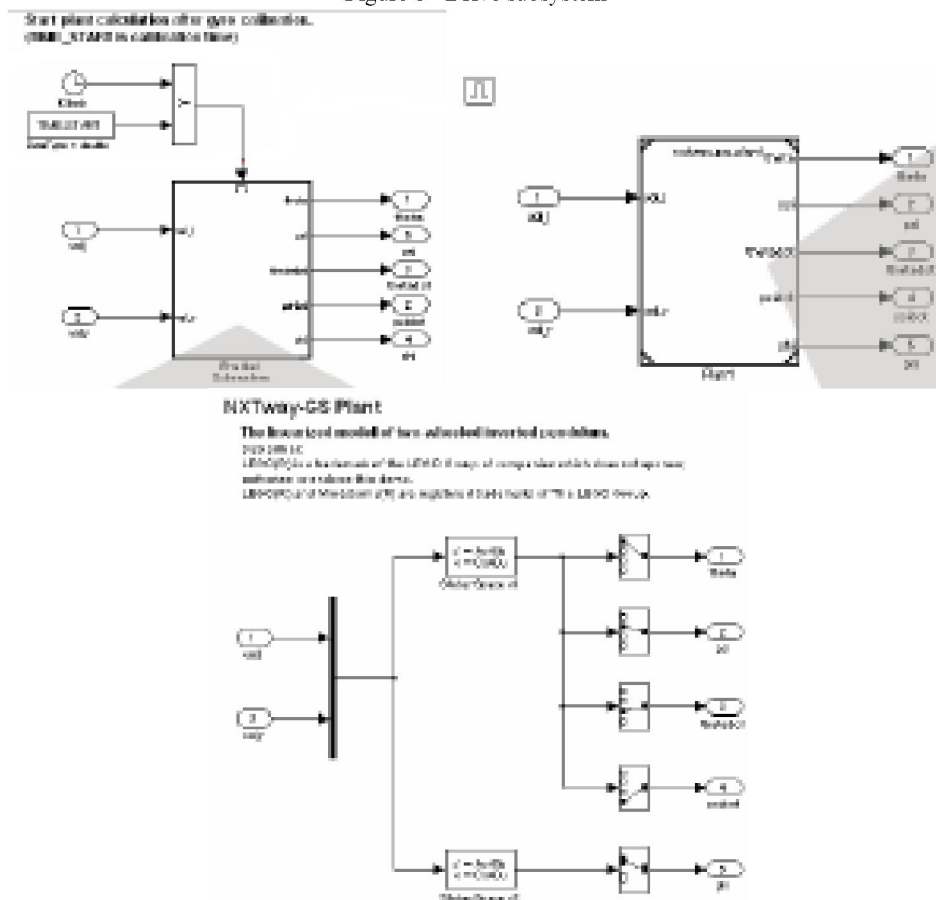
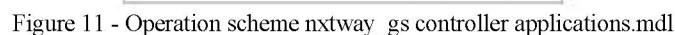
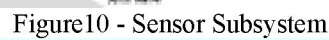


Figure 9 - Model Subsystem



Block “task\_tsl” serves for calibration and balancing the gyroscope and for controlling the sound level and writing data. Balancing and control start after calibrating the Osprey Gear. The calibration time is saved as “time\_start”.

Further, in the constructed schemes, the subsystems of balancing and control are presented. In the circuit shown in Figure 17 is a block “DiscreteDerivativeBlock”, which calculates the time constant of reverse differentiation block and “DiscreteIntegratorBlock”, which calculates the time integral by Euler method.



## Shared Data

Data Store Memory is used as a shared data between tasks.

<b>flag_ready</b> DataType = boolean	<b>drive mode flag</b> 1 : autonomous drive 0 : remote control drive	<b>is_battery</b> DataType = int32	<b>average battery voltage</b>
<b>flag_start</b> DataType = boolean	<b>start time flag</b> 1 : gyro calibration is finished 0 : gyro calibration is not finished	<b>gyro_offset</b> DataType = int32	<b>gyro offset (zero point value)</b>
<b>flag_auto</b> DataType = boolean	<b>autonomous time flag</b> 1 : autonomous drive is ready 0 : autonomous drive is not ready	<b>task_time</b> DataType = uint32	<b>program start time</b>
<b>flag_avoid</b> DataType = boolean	<b>avoidance flag</b> 1 : NDT way-GS is avoiding obstacle 0 : NDT way-GS is not avoiding obstacle		

Figure 12 - Distributed data blocks

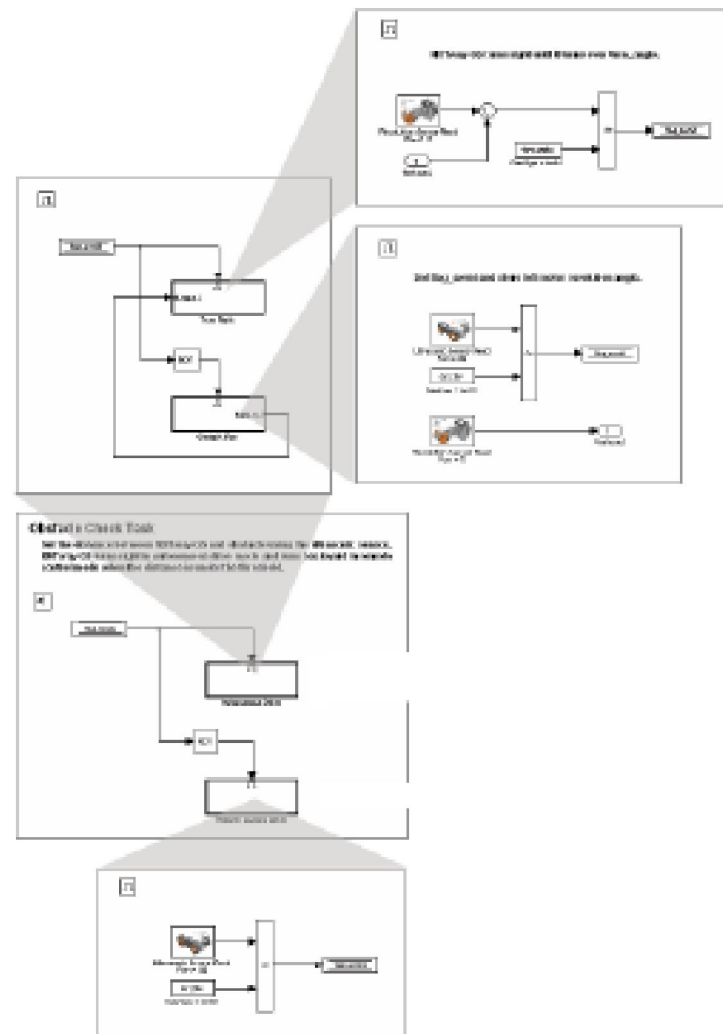


Figure13 - The task\_ts2 subsystem responds for detecting and avoiding robbery

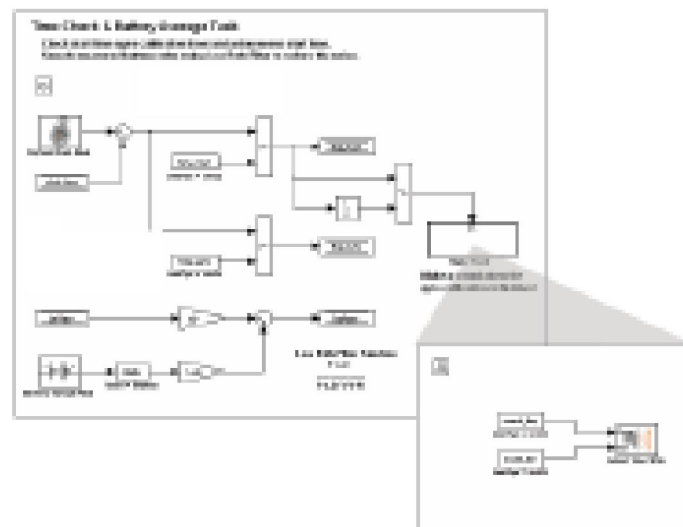


Figure 14 - The task\_ts3 subsystem is responsible for counting time, and check the battery level of the robot

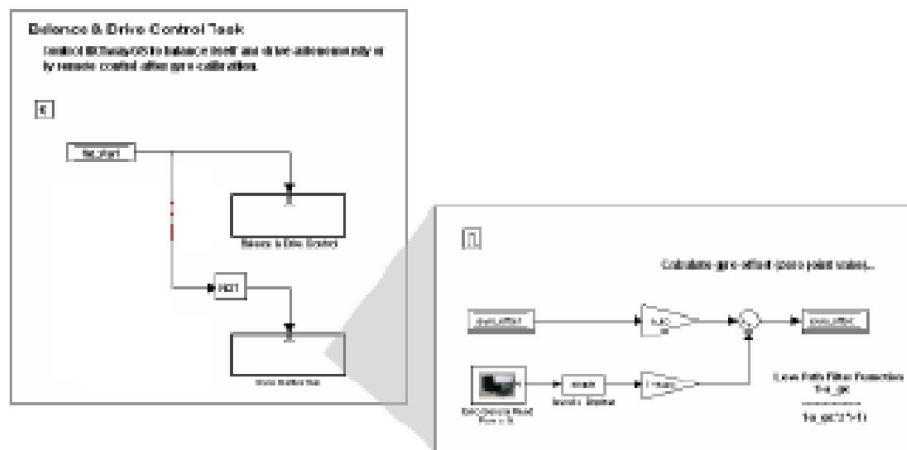


Figure15 - The task\_ts1 subsystem is used to calibrate the gyroscope and balancing, as well as for managing and recording data

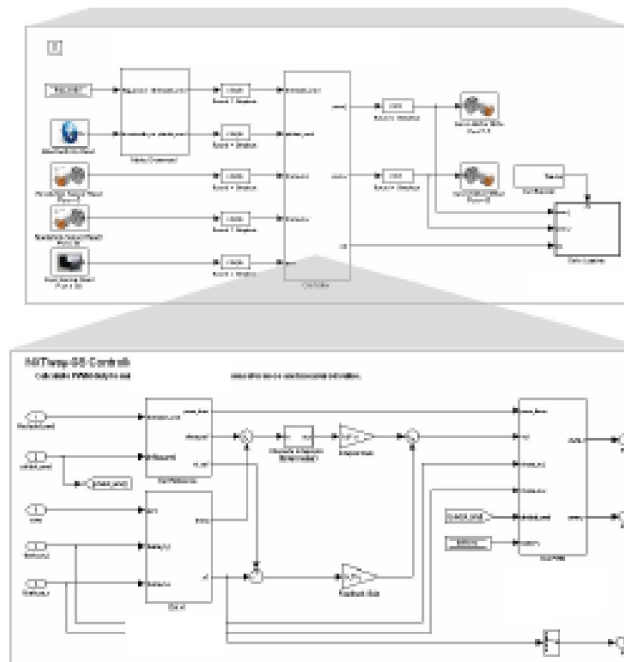


Figure16 - Controller model for control in balance mode



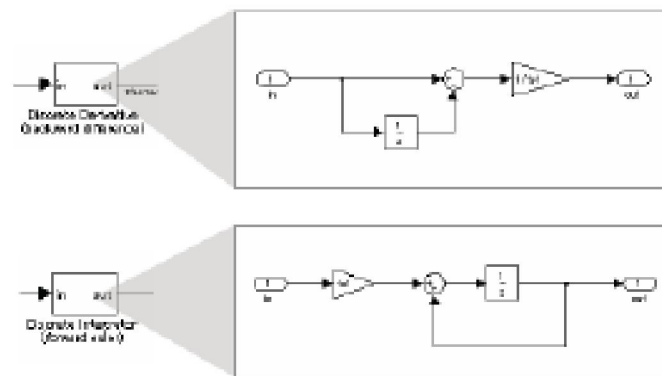


Figure17 - Blocks of the controllers «Discrete Derivative» and «Discrete Integrator Block»

Figure 17 also contains the blocks responsible for the calculation of the signal level, and with the use of a low pass filter for reducing surges caused by abrupt changes in speed of the generated signal. Figure 18 shows the method for calculating the generated controls.

Subsystem shown in Figure 19 calculates the state of the system using the sensor output signals. Long gyro data is used to remove "girodriфта" (gidrodreyfa), and a low pass filter is used for removing away move speed signal. The subsystem shown in Figure 20 is responsible for calculating the supply of the required power to the servo drives.

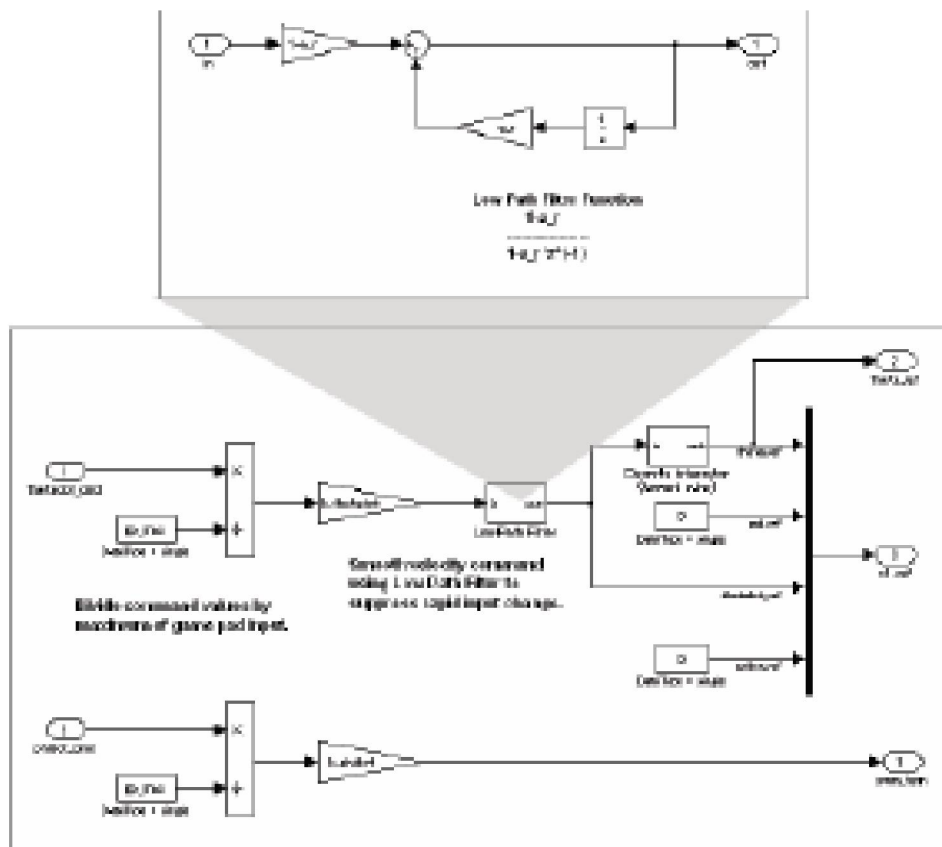


Figure 18 - Procedure for Calculating p and controls generated

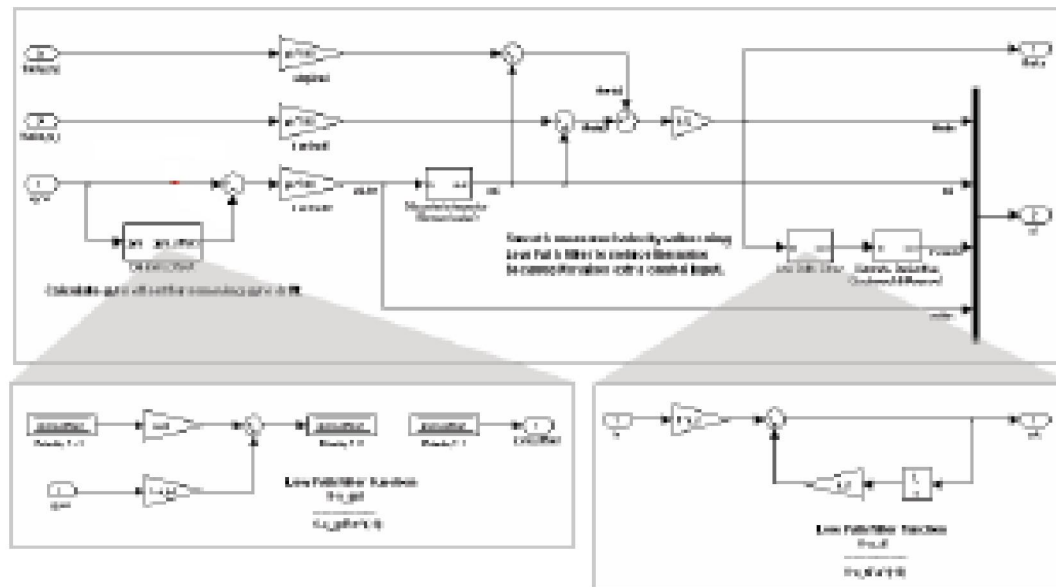


Figure 19 - Monitoring and monitoring the state of the model as a closed system

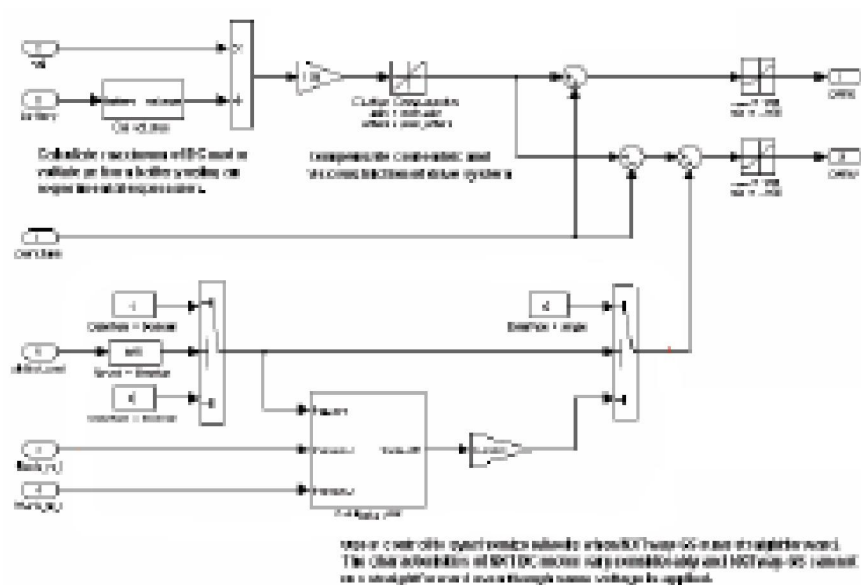


Figure 20 - Procedure for calculating p and the power supplied to the robot servo

**The simulation results.** The use of the utility “NXT GamePad” can register and record the value of an angle of inclination of the robot of the gyroscope and the robot regarding to the beginning of the movement using the values of the encoder of one of the servomotors. Figures 21 and 22 show the results of experimental research in the form of a graph of the data obtained by balancing the robot in a steady state and in a motion, respectively.

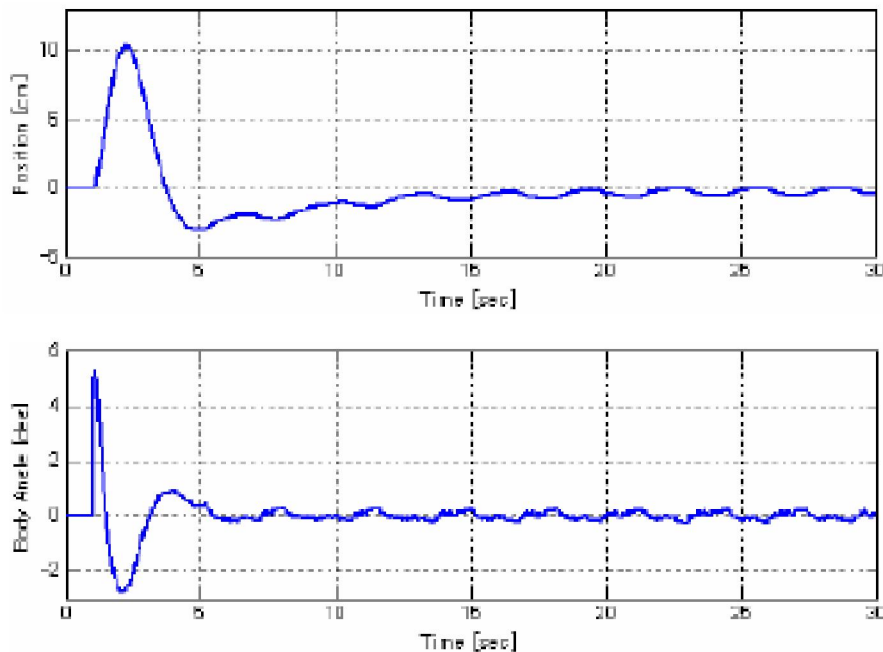


Figure 21 - Model results in a steady state

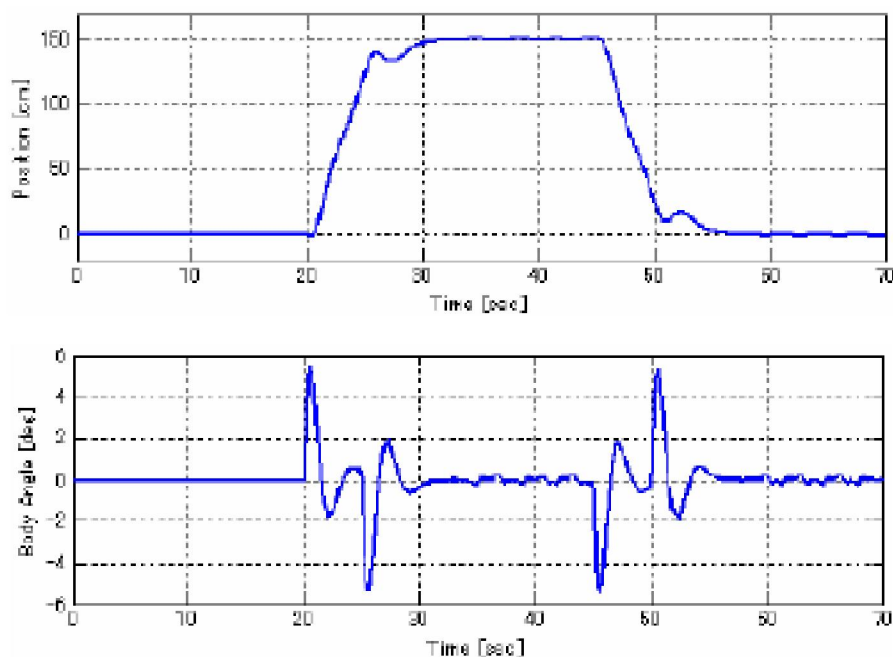


Figure 22 - Simulation results in motion

**Findings.** The article addresses the problems of stability of a balancing robot in motion in accordance with the laws of TAU. The stability of a closed system on the basis of feedback has been investigated. The coefficients were synthesized using the following methods: calculation by the desired roots and the linear quadratic regulator method. According to the defined parameters of the PID controller, functional diagrams are compiled for controlling the robot servos. The results of experimental studies of balancing a robot in static and dynamic conditions were obtained using the NINXT GamePad utility, taking into account the value of the tilt angle of the robot from the gyroscope relative to the start of movement, using the encoder value of one of the servomotors. Registered statistics for specific values of the parameters of the controller of the robot show the degree of compliance with its stability when the robot moves in the closed state.

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### ИССЛЕДОВАНИЕ УСТОЙЧИВОСТИ РЕГУЛЯТОРА БАЛАНСИРУЮЩЕГО РОБОТА NI MINDSTORMS

**Аннотация.** В статье представлены результаты исследования устойчивого состояния балансирующего робота, когда управление осуществляется в замкнутом состоянии. Синтез коэффициентов регулятора осуществлялся оценкой корня характеристического уравнения и линейного квадратичного регулятора. При действии ПИД-регулятора составлены алгоритмы управления сервоприводами робота. Результаты проведенных экспериментальных исследований позволили построить переходные характеристики в замкнутой системе управления роботом при балансировании состояния робота на месте и в движении.

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### РОБОТ NI MINDSTORMS РЕГУЛЯТОРДЫҢ ТҰРАҚТЫЛЫҒЫН ЗЕРТТЕУ ТЕНДЕСТІРУ

**Аннотация.** Мақалада тендестіру роботының тұрақты күйін зерттеудің нәтижелері келтірілген, ол бақылау жабық жағдайда орындалады. Реттеуші коэффициенттерді синтездеу тәндік тендеудің түбірін және сызықтық квадраттық реттегішті бағалау арқылы жүзеге асырылды. PID контроллерінің әрекеті бойынша робот серверлерін басқару алгоритмдері жасалады. Эксперименттік зерттеулердің нәтижелері біз роботтың жай-күйі мен қозғалу жағдайын теңдестіру кезінде жабық циклдық роботты басқару жүйесінде өтпелі сипаттамаларды құруға мүмкіндік берді.

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